

Work, Energy & Power — Complete Formula Card

- The work–energy theorem is the shortcut: compare before/after states, skip the path
- Three energy stores in JEE problems: height (mgh), springs ($\frac{1}{2}kx^2$), motion ($\frac{1}{2}mv^2$)
- Friction is a leak, not a store — it converts mechanical energy to heat, $F \cdot d$ at a time

What	Formula	Remember
Work	$W = Fd \cdot \cos\theta$	perpendicular = zero; against motion = negative
Kinetic energy	$\frac{1}{2}mv^2$	square! double speed $\times 4$
Work–energy theorem	$W_{\text{total}} = \Delta KE$	before/after only — path-free
Height PE	mgh	choose one zero level
Spring PE	$\frac{1}{2}kx^2$	stretch squared; metres!
Energy conservation	$KE + PE = \text{constant (gravity/springs)}$	friction leak = $F \cdot d \rightarrow \text{heat}$
Drop speed	$v = \sqrt{2gh}$	no mass anywhere
Loop minimums	$v_{\text{top}} = \sqrt{gR}$; $v_{\text{bottom}} = \sqrt{5gR}$; $h = 2.5R$	gravity helps at the top
Power	$P = W/t = Fv$	watts; 1 hp = 746 W
Efficiency	$\text{useful} \div \text{input}$	always $< 100\%$
Collisions	momentum always survives	sticking = max KE loss; equal-mass elastic = swap
Variable force	work = area under F – d graph	$\frac{1}{2}kx^2$ is the triangle
PE curves	valley = stable, hill = unstable	slope = force

Mistakes to avoid

- Never assume constant force when told it varies — use area under the F – d graph
- Valley = stable, hill = unstable — draw the ball, feel the answer
- Efficiency direction: $\text{input} = \text{useful} \div \text{efficiency}$ (bigger); $\text{output} = \text{input} \times \text{efficiency}$ (smaller)
- Human power is overestimated: we sustain ~ 100 – 150 W — light bulbs, not engines